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MADALGO seminar by Jeff M. Phillips, University of Utah

## Comparing Distributions and Shapes with the Kernel Distance

### Abstract:

The kernel distance is the metric formed using a kernel (or similarity function). Specifically, given a positive definite  $K: R^d \times R^d \rightarrow R$ , then for two points sets  $P, Q$  in  $R^d$  the kernel distance is defined:

$$D_K(P, Q) = \sqrt{K(P, P) + K(Q, Q) - 2K(P, Q)}$$

Where

$$K(P, Q) = \sum_{p \in P} \sum_{q \in Q} K(p, q).$$

This definition generalizes naturally to shapes (curves, surfaces), distributions, clusters, graphs, and trees. In the past 5 years or so, a flurry of work in medical imaging (where  $D_K$  is called the current distance) and machine learning (where  $D_K$  is called maximum mean discrepancy or MMD) has shown the practicality of this measure as well as its favorable relation to more classic measures such as EMD.

In this talk, I will provide the first rigorous algorithmic analysis of the kernel distance. I first will reduce the kernel distance on smooth shapes and distributions with bounded error to the kernel distance on finite point sets. Then I will produce near-linear algorithms on point sets that preserves the same bounded error, beating the naive quadratic runtime bound.

Joint work with:

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